

**Solving Systems of Equations by Substitution**  
 Unit 4: Systems

**Solve each of the following systems by using SUBSTITUTION:**

$\begin{aligned} 1. \quad y &= 8x - 13 \\ y &= x + 1 \end{aligned}$ $(2, 3)$	$\begin{aligned} 2. \quad y &= -7x - 11 \\ y &= 10x + 23 \end{aligned}$ $(-2, 3)$
$\begin{aligned} 3. \quad y &= -7x - 8 \\ y &= 7x + 6 \end{aligned}$ $(-1, -1)$	$\begin{aligned} 4. \quad y &= -7x + 4 \\ y &= 4x + 4 \end{aligned}$ $(0, 4)$
$\begin{aligned} 5. \quad y &= -8x + 9 \\ y &= 3x - 2 \end{aligned}$ $(1, 1)$	$\begin{aligned} 6. \quad y &= 5x + 13 \\ -4x + 2y &= 20 \end{aligned}$ $(-1, 8)$
$\begin{aligned} 7. \quad -6x - 8y &= 2 \\ y &= 5 \end{aligned}$ $(-7, 5)$	$\begin{aligned} 8. \quad y &= -9x - 27 \\ -9x - y &= 27 \end{aligned}$ $\text{Infinite Solutions or ALL REAL NUMBERS}$
$\begin{aligned} 9. \quad 8x - 8y &= 0 \\ y &= -3x - 20 \end{aligned}$ $(-5, -5)$	$\begin{aligned} 10. \quad y &= 8x - 6 \\ 9x - 9y &= -9 \end{aligned}$ $(1, 2)$

$$\begin{aligned}11. \quad & x + y = 7 \\& 2x + 4y = 12\end{aligned}$$

$$(8, -1)$$

$$\begin{aligned}12. \quad & -8x - y = -5 \\& -5x + y = 5\end{aligned}$$

$$(0, 5)$$

$$\begin{aligned}13. \quad & 9x - 7y = -12 \\& x + 3y = 10\end{aligned}$$

$$(1, 3)$$

$$\begin{aligned}14. \quad & 5x + y = 0 \\& -7x - 3y = -8\end{aligned}$$

$$(-1, 5)$$

$$\begin{aligned}15. \quad & x - 3y = 10 \\& -2x + 2y = -8\end{aligned}$$

$$(1, -3)$$

$$\begin{aligned}16. \quad & -2x - 4y = -22 \\& 2x - 2y = -26\end{aligned}$$

$$(-5, 8)$$

$$\begin{aligned}17. \quad & 10x + 9y = 20 \\& -3x - 4y = -6\end{aligned}$$

$$(2, 0)$$

$$\begin{aligned}18. \quad & -5x - 3y = -5 \\& 9x + 6y = 3\end{aligned}$$

$$(7, -10)$$

$$\begin{aligned}19. \quad & 4x - y = 6 \\& 4x - 3y = 26\end{aligned}$$

$$(-1, -10)$$

$$\begin{aligned}20. \quad & -7x + 9y = 12 \\& -9x + 3y = 24\end{aligned}$$

$$(-3, -1)$$

$$\textcircled{1} \quad y = 8x - 13 \quad y = x + 1$$

$$\text{So } 8x - 13 = x + 1$$

$$\begin{array}{r} -x \\ \hline 7x - 13 = 1 \end{array}$$

$$\begin{array}{r} +13 \quad +13 \\ \hline 7x = 14 \end{array}$$

$$\frac{7x}{7} = \frac{14}{7}$$

$$x = 2$$

Plug into equation above

$$y = 2 + 1$$

$$y = 3$$

Solution  
 $(2, 3)$

$$\textcircled{2} \quad y = -7x - 11 \quad y = 10x + 23$$

$$\begin{array}{r} -7x - 11 = 10x + 23 \\ -10x \quad -10x \\ \hline -17x - 11 = 23 \\ +11 \quad +11 \\ \hline -17x = 34 \\ -17 \quad -17 \end{array}$$

Plug into equation above

$$x = -2$$

Solution

$$(-2, 3)$$

$$y = -7(-2) - 11$$

$$y = 14 - 11$$

$$y = 3$$

$$\textcircled{3} \quad y = -7x - 8 \quad y = 7x + 6$$

$$\begin{array}{r} -7x - 8 = 7x + 6 \\ +7x \quad +7x \\ \hline -8 = 14x + 6 \\ -6 \quad -6 \\ \hline -14 = 14x \\ -14 \quad -14 \end{array}$$

$$-1 = x$$

Plug into equation above

$$y = 7(-1) + 6$$

$$y = -7 + 6$$

$$y = -1$$

Solution  
 $(-1, -1)$

$$(4) \quad y = -7x + 4 \quad y = 4x + 4$$

$$\begin{array}{r} -7x + 4 = 4x + 4 \\ +7x \qquad +7x \\ \hline 4 = 11x + 4 \\ -4 \qquad -4 \\ \hline 0 = 11x \end{array}$$

Solution

$$\boxed{(0, 4)}$$

$$\boxed{0 = x}$$

Plug into  $y = 4x + 4$

$$\begin{aligned} y &= 4(0) + 4 \\ y &= 0 + 4 \\ y &= 4 \end{aligned}$$

$$(5) \quad y = -8x + 9 \quad y = 3x - 2$$

$$\begin{array}{r} -8x + 9 = 3x - 2 \\ +8x \qquad +8x \\ \hline 9 = 11x - 2 \\ +2 \qquad +2 \\ \hline 11 = 11x \end{array}$$

Solution

$$\boxed{(1, 1)}$$

$$\boxed{1 = x}$$

Plug into  $y = 3x - 2$

$$\begin{aligned} y &= 3(1) - 2 \\ y &= 3 - 2 \\ y &= 1 \end{aligned}$$

$$(6) \quad y = 5x + 13 \quad -4x + 2y = 20$$

Replace  $x = -1$

$$y = 5(-1) + 13$$

$$y = -5 + 13$$

$$\boxed{y = 8}$$

Solution

$$\boxed{(-1, 8)}$$

$$\begin{array}{r} -2x + y = 10 \\ -2x + 5x + 13 = 10 \\ 3x + 13 = 10 \end{array}$$

$$\begin{array}{r} -13 \qquad -13 \\ \hline 3x = -3 \end{array}$$

$$\boxed{x = -1}$$

$$(7) \quad -6x - 8y = 2$$

$$-6x - 8(5) = 2$$

$$\begin{array}{r} -6x - 40 = 2 \\ +40 \quad +40 \\ \hline -6x = 42 \\ -6 \quad -6 \end{array}$$

$$x = -7$$

$$y = 5$$

Solution

$$(-7, 5)$$


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$$(8) \quad y = -9x - 27$$

ALL REAL NUMBERS

OR

Infinite Solutions

$$-9x - y = 27$$

$$-9x - (-9x - 27) = 27$$

$$-9x + 9x + 27 = 27$$

$$27 = 27$$


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$$(9) \quad 8x - 8y = 0$$

$$8x - 8(-3x - 20) = 0$$

$$8x + 24x + 160 = 0$$

$$\begin{array}{r} 32x + 160 = 0 \\ -160 \quad -160 \\ \hline 32x = -160 \\ 32 \quad 32 \end{array}$$

$$x = -5$$

$$y = -3x - 20$$

$$y = -3(-5) - 20$$

$$y = 15 - 20$$

$$y = -5$$

Solution

$$(-5, -5)$$


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$$(10) \quad y = 8x - 6$$

$$y = 8(1) - 6$$

$$y = 8 - 6$$

$$y = 2$$

Solution

$$(1, 2)$$

$$\frac{9x - 9y}{9} = \frac{-9}{9}$$

$$x - y = -1$$

$$x - (8x - 6) = -1$$

$$x - 8x + 6 = -1$$

$$\begin{array}{r} -7x + 6 = -1 \\ -6 \quad -6 \\ \hline -7x = -7 \end{array}$$

$$x = 1$$


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$$(11) \quad x + y = 7$$

$$-2y + 6 + y = 7$$

$$\begin{array}{r} -y + 6 = 7 \\ -6 \quad -6 \end{array}$$

$$\begin{array}{r} -y = 1 \\ -1 \quad -1 \end{array}$$

$$\boxed{y = -1}$$

Solution

$$\boxed{(8, -1)}$$

$$\frac{2x + 4y}{2} = \frac{12}{2}$$

$$x + 2y = 6$$

$$\begin{array}{r} -2y \quad -2y \\ \hline \end{array}$$

$$x = \boxed{-2y + 6}$$

$$x = -2(-1) + 6$$

$$x = 2 + 6$$

$$\boxed{x = 8}$$

$$(12) \quad -8x - y = -5$$

$$-8x - (5x + 5) = -5$$

$$-8x - 5x - 5 = -5$$

$$\begin{array}{r} -13x - 5 = -5 \\ +5 \quad +5 \end{array}$$

$$\begin{array}{r} -13x = 0 \\ -13 \quad -13 \end{array}$$

$$\boxed{x = 0}$$

Solution

$$\boxed{(0, 5)}$$

$$\begin{array}{r} -5x + y = 5 \\ +5x \quad +5x \end{array}$$

$$y = \boxed{5x + 5}$$

$$y = 5(0) + 5$$

$$y = 0 + 5$$

$$\boxed{y = 5}$$

$$(13) \quad 9x - 7y = -12$$

$$9(-3y + 10) - 7y = -12$$

$$-27y + 90 - 7y = -12$$

$$\begin{array}{r} -34y + 90 = -12 \\ -90 \quad -90 \end{array}$$

$$\begin{array}{r} -34y = -102 \\ -34 \quad -34 \end{array}$$

$$\boxed{y = 3}$$

Solution

$$\boxed{(1, 3)}$$

$$x + 3y = 10$$

$$\begin{array}{r} -3y \quad -3y \\ \hline \end{array}$$

$$x = \boxed{-3y + 10}$$

$$x = -3(3) + 10$$

$$x = -9 + 10$$

$$\boxed{x = 1}$$

$$(14) \quad \begin{array}{r} 5x + y = 0 \\ -5x \quad -5x \end{array}$$

$$y = \boxed{-5x}$$

$$y = -5(-1)$$

$$\boxed{y = 5}$$

Solution

$$\boxed{(-1, 5)}$$

$$-7x - 3y = -8$$

$$-7x - 3(-5x) = -8$$

$$-7x + 15x = -8$$

$$\frac{8x}{8} = \frac{-8}{8}$$

$$\boxed{x = -1}$$

$$(15) \quad x - 3y = 10$$

$$x - 3(x-4) = 10$$

$$x - 3x + 12 = 10$$

$$\begin{array}{r} -2x + 12 = 10 \\ -12 \quad -12 \end{array}$$

$$\begin{array}{r} -2x = -2 \\ -2 \quad -2 \end{array}$$

$$\boxed{x = 1}$$

Solution  
 $\boxed{(1, -3)}$

$$\frac{-2x + 2y}{2} = \frac{-8}{2}$$

$$\begin{array}{r} -x + y = -4 \\ +x \quad +x \end{array}$$

$$y = \boxed{x - 4}$$

$$y = 1 - 4$$

$$\boxed{y = -3}$$

$$(16) \quad \frac{-2x - 4y}{-2} = \frac{-22}{-2}$$

$$x + 2y = 11$$

$$y - 13 + 2y = 11$$

$$\begin{array}{r} 3y - 13 = 11 \\ +13 \quad +13 \end{array}$$

$$\frac{3y}{3} = \frac{24}{3}$$

$$\boxed{y = 8}$$

Solution  
 $\boxed{(-5, 8)}$

$$\frac{2x - 2y}{2} = \frac{-26}{2}$$

$$\begin{array}{r} x - y = -13 \\ +y \quad +y \end{array}$$

$$x = \boxed{y - 13}$$

$$x = 8 - 13$$

$$\boxed{x = -5}$$

$$(17) \quad 10x + 9y = 20$$

$$\begin{array}{r} -9y \quad -9y \end{array}$$

$$\frac{10x}{10} = \frac{-9y}{10} + \frac{20}{10}$$

$$x = \boxed{\frac{-9}{10}y + 2}$$

$$x = \frac{-9}{10}(0) + 2$$

$$x = 0 + 2$$

$$\boxed{x = 2}$$

Solution  
 $\boxed{(2, 0)}$

$$-3x - 4y = -6$$

$$-3\left(-\frac{9}{10}y + 2\right) - 4y = -6$$

$$10 \left[ \frac{27}{10}y - 6 - 4y = -6 \right] \text{ } 10$$

$$27y - 60 - 40y = -60$$

$$\begin{array}{r} -13y - 60 = -60 \\ +60 \quad +60 \end{array}$$

$$\frac{-13y}{-13} = \frac{0}{-13}$$

$$\boxed{y = 0}$$

$$(18) \begin{array}{r} -5x - 3y = -5 \\ +3y \quad +3y \\ \hline -5x = \frac{3y}{-5} - \frac{5}{-5} \\ x = \boxed{\frac{-3}{5}y + 1} \\ x = \frac{-3}{5}(-\frac{10}{1}) + 1 \\ x = \frac{30}{5} + 1 \\ x = 6 + 1 \\ \boxed{x = 7} \end{array}$$

Solution  
 $\boxed{(7, -10)}$

$$\begin{array}{r} 9x + 6y = 3 \\ 9(-\frac{3}{5}y + 1) + 6y = 3 \\ 5 \left[ -\frac{27}{5}y + 9 + 6y = 3 \right] \cancel{5} \\ -27y + 45 + 30y = 15 \\ 3y + 45 = 15 \\ \cancel{-45} \quad \cancel{-45} \\ 3y = -30 \\ \cancel{3} \quad \cancel{3} \\ \boxed{y = -10} \end{array}$$

$$(19) \begin{array}{r} 4x - y = 6 \\ -4x \quad -4x \\ \hline -y = \frac{-4x}{-1} + \frac{6}{-1} \\ y = \boxed{4x - 6} \\ y = 4(-1) - 6 \\ y = -4 - 6 \\ \boxed{y = -10} \end{array}$$

Solution  
 $\boxed{(-1, -10)}$

$$\begin{array}{r} 4x - 3y = 26 \\ 4x - 3(4x - 6) = 26 \\ 4x - 12x + 18 = 26 \\ -8x + 18 = 26 \\ \cancel{-18} \quad \cancel{-18} \\ -8x = 8 \\ \cancel{-8} \quad \cancel{-8} \\ \boxed{x = -1} \end{array}$$

$$(20) \begin{array}{r} -7x + 9y = 12 \\ -7x + 9(3x + 8) = 12 \\ -7x + 27x + 72 = 12 \\ 20x + ?? = 12 \\ \cancel{-72} \quad \cancel{-72} \\ \frac{20x}{20} = \frac{-60}{20} \\ x = \boxed{-3} \end{array}$$

Solution  
 $\boxed{(-3, -1)}$

$$\begin{array}{r} -9x + 3y = 24 \\ +9x \quad +9x \\ \hline 3y = \frac{9x}{3} + \frac{24}{3} \\ 3y = \boxed{3x + 8} \\ y = 3(-3) + 8 \\ y = -9 + 8 \\ \boxed{y = -1} \end{array}$$